



basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

NATIONAL SENIOR CERTIFICATE

GRADE 12

TECHNICAL MATHEMATICS P2

MARKING GUIDELINES

EXEMPLAR 2018

MARKS: 150

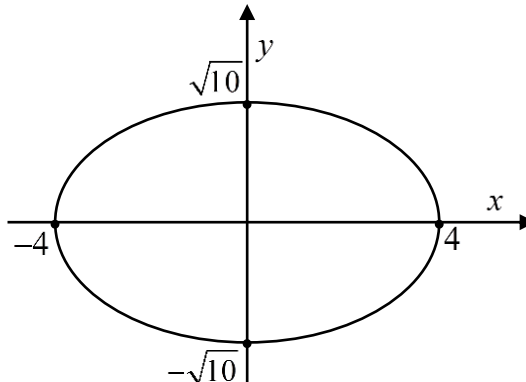
These marking guidelines consist of 14 pages

QUESTION 1

1.1	$AD = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ $= \sqrt{(5-1)^2 + (-2-4)^2}$ $= \sqrt{52}$ $= 2\sqrt{13}$	✓ Substitution in correct formula ✓ Simplification ✓ $2\sqrt{13}$ simplified surd (3)
1.2	$M\left(\frac{x_1 + x_2}{2}; \frac{y_1 + y_2}{2}\right)$ $M\left(\frac{1+5}{2}; \frac{4-2}{2}\right)$ $M(3; 1)$	✓ Substitution ✓ $M(3; 1)$ (2)
1.3	$m_{AB} = \frac{y_2 - y_1}{x_2 - x_1}$ $= \frac{1-4}{-3-1}$ $= \frac{3}{4}$ $AB \parallel MC$ $m_{MC} = \frac{3}{4}$ $y - y_1 = m(x - x_1) \quad \text{or} \quad y = mx + c$ $y - 1 = \frac{3}{4}(x - 3) \quad 1 = \frac{3}{4}(3) + c$ $-3x + 4y + 5 = 0 \quad c = \frac{4-9}{4} = -\frac{5}{4}$ $\text{or } 3x + -4y - 5 = 0 \quad y = \frac{3}{4}x - \frac{5}{4}$ $-3x + 4y + 5 = 0$	✓ Substitution in correct formula ✓ Gradient of MC ✓ Substitution in correct formula ✓ Simplification ✓ Correct answer in correct form (5)
1.4	$\tan \alpha = \frac{3}{4}$ $\alpha \approx 36,87^\circ$	✓ $\tan \alpha = \frac{3}{4}$ ✓ $36,87^\circ$ (2)

1.5	$m_{AD} = \frac{y_2 - y_1}{x_2 - x_1}$ $= \frac{-2 - 4}{5 - 1}$ $= \frac{-3}{2}$ $\tan \beta = \frac{-3}{2}$ $\beta \approx 123,69^\circ$ $\hat{B}AD = 123,69^\circ - 36,87^\circ \quad \text{ext } \angle \text{ of } \Delta$ $= 86,82^\circ$	$\checkmark \frac{-3}{2}$ $\checkmark \beta = 123,69^\circ$ $\checkmark 123,69^\circ - 36,87^\circ$ $\checkmark 86,82^\circ$ (4)
		[16]

QUESTION 2

2.1.1	$x^2 + y^2 = r^2$ $r^2 = (10)^2 + (-4)^2$ $\therefore r = \sqrt{116} = 2\sqrt{29}$	✓ Substitution. ✓ $\sqrt{116} = 2\sqrt{29}$ (2)
2.1.2	$m_{OH} = m_{OF} = \frac{0 - (-4)}{0 - 10}$ $= -\frac{4}{10}$ $= -\frac{2}{5}$	✓ Substitution. ✓ $-\frac{2}{5}$ (2)
2.1.3	$m_{GH} = \frac{5}{2}$ $(m_{GH} \times m_{OH} = -1)$ By symmetry H(-10; 4) $y - y_1 = m(x - x_1)$ or $y = mx + c$ $y - 4 = \frac{5}{2}(x + 10)$ $4 = \frac{5}{2}(-10) + c$ $y = \frac{5}{2}x + 29$ $c = 29$ $y = \frac{5}{2}x + 29$	✓ m_{GH} ✓ H(-10; 4) ✓ Substitution of H ✓ Equation (4)
2.2		✓ Both x-intercepts ✓ Both y-intercepts ✓ Shape (3)
		[11]

QUESTION 3

3.1.1	$OP^2 = (12)^2 + (-5)^2$ $\therefore OP = 13 \text{ units}$	$\checkmark OP = 13 \text{ units}$ (1)
3.1.2	$5 \cot \theta - 13 \cos \theta$ $= 5 \left(\frac{12}{-5} \right) - 13 \left(\frac{12}{13} \right)$ $= -24$	$\checkmark \frac{12}{-5}$ $\checkmark \frac{12}{13}$ $\checkmark$ Simplification (3)
3.1.3	$\operatorname{cosec}^2 x - 1$ $= \left(\frac{13}{-5} \right)^2 - 1$ $= \frac{144}{25}$ $\text{or } \operatorname{cosec}^2 x - 1 = \cot^2 x$ $= \left(\frac{12}{-5} \right)^2$ $= \frac{144}{25}$	$\checkmark \left(\frac{13}{-5} \right)^2 \text{ or } \left(\frac{12}{-5} \right)^2$ $\checkmark$ Simplification (2)
3.2	$\sec(a - b)$ $= \sec(2,659 - 1,112)$ $= \sec 1,547$ $= \frac{1}{\cos 1,547}$ $\approx 42,03$	$\checkmark$ Substitution $\checkmark$ Reciprocal $\checkmark$ Simplification using radians (3)
		[9]

QUESTION 4

4.1	$\frac{\sin(360^\circ - x) \cdot \cos(180^\circ - x) \cdot \tan 120^\circ}{\cos^2 x \cdot \sin \frac{5\pi}{6}}$ $= \frac{(-\sin x) \cdot (-\cos x) \cdot (-\tan 60^\circ)}{\cos^2 x \cdot \sin \frac{\pi}{6}}$ $= \frac{-\sin x \cdot \cos x \cdot -\sqrt{3}}{\cos^2 x \cdot \frac{1}{2}}$ $= \frac{2\sqrt{3} \sin x}{\cos x}$ $= 2\sqrt{3} \tan x$	$\checkmark -\sin x$ $\checkmark -\cos x$ $\checkmark -\tan 60^\circ$ $\checkmark \sin \frac{\pi}{6}$ $\checkmark -\sqrt{3} \text{ and } \frac{1}{2}$ $\checkmark \text{ simplification}$ $\checkmark \tan x$
4.2	$\cos^2 3x$	$\checkmark \cos^2 3x$ (7)
4.3	$LHS = \frac{\sin x}{\cos x} (\sin x)$ $= \frac{\sin^2 x}{\cos x}$ $RHS = \sec x - \cos x$ $= \frac{1}{\cos x} - \cos x$ $= \frac{1 - \cos^2 x}{\cos x}$ $= \frac{\sin^2 x}{\cos x}$ $= LHS$	$\checkmark \frac{\sin x}{\cos x}$ $\checkmark \frac{1}{\cos x}$ $\checkmark \frac{1 - \cos^2 x}{\cos x}$ $\checkmark \sin^2 x$
4.4	$\operatorname{cosec} 2x = 2,114$ $\sin 2x = \frac{1}{2,114}$ $2x = \sin^{-1}\left(\frac{1}{2,114}\right)$ $2x = \sin^{-1}\left(\frac{1}{2,114}\right)$ $2x \approx 28,23^\circ \quad \text{or} \quad 2x \approx 180^\circ - 28,23^\circ$ $x \approx 14,12^\circ \quad \text{or} \quad x \approx 75,89^\circ$	$\checkmark \text{ using reciprocal}$ $\checkmark \text{ inverse}$ $\checkmark \text{ value of } x$ $\checkmark \text{ another value of } x$
		(4)
		[16]

QUESTION 5

5.1	$\sin 55^\circ = \frac{50}{AC}$ $AC = \frac{50}{\sin 55^\circ}$ $\approx 61\text{m}$	✓ Definition ✓ AC subject ✓ 61m (3)
5.2	$AD \approx 61\text{ m}$ $DC^2 = AC^2 + AD^2 - 2AC \cdot AD \cos 65^\circ$ $DC^2 = (61)^2 + (61)^2 - 2(61)(61) \cos 65^\circ$ $DC \approx 66\text{ m}$	✓ $AD \approx 61\text{ m}$ ✓ Using cosine rule ✓ Substitution ✓ 66 m (4)
5.3	$BD = \sqrt{AD^2 - AB^2}$ $= \sqrt{(61)^2 - (50)^2} \quad \text{OR} \quad \tan 55^\circ = \frac{50}{BD}$ $\approx 35\text{ m} \quad \quad \quad = 35\text{ m}$ $\therefore \text{area of } \triangle BDC = \frac{1}{2}(35)(66) \sin \hat{BDC} = 563$ $\sin \hat{BDC} = \frac{563}{\frac{1}{2}(35)(66)}$ $\therefore \hat{BDC} = \sin^{-1}\left(\frac{563}{\frac{1}{2}(35)(66)}\right)$ $= 29,17^\circ$	✓ Using Pythagoras theorem or tan ✓ $BD = 35\text{ m}$ ✓ Substitution in area formula ✓ Area = 563 $\checkmark \sin \hat{BDC} = \frac{563}{\frac{1}{2}(35)(66)}$ ✓ Simplification (6)
		[13]

QUESTION 6

6.1		$f(x)$ ✓ x -intercepts ✓ y -intercept ✓ Shape $g(x)$ ✓ y -intercept ✓ Turning points ✓ Shape (6)
6.2	2	✓ 2 (1)
6.3	360°	✓ 360° (1)
6.4	$60^\circ < x < 240^\circ$	✓ ✓ Answer with correct notation (2)
		[10]

QUESTION 7

7.1	the angle in the alternate segment	✓ Correct statement (1)
7.2.1	$\hat{R}_2 = \hat{S}_1 = 38^\circ$ tan – chord theorem	✓ Statement ✓ Reason (2)
7.2.2	$\hat{M}_1 = 2\hat{R}_2 = 76^\circ$ $\angle$ at center = $2\angle$ at circum	✓ Statement ✓ Reason (2)
7.2.3.	$\hat{S}_2 = 90^\circ - 38^\circ = 52^\circ$ tan $\perp$ radius	✓ Statement ✓ Reason (2)
7.2.4	$\hat{R}_1 = 90^\circ$ $\angle$ in a semi – circle $\hat{Q}_1 = \hat{S}_1 = 38^\circ$ tan– chord theorem $\therefore \hat{Q}_2 = 180^\circ - (17^\circ + 90^\circ + 38^\circ)$ sum of $\angle$'s of a Δ $= 35^\circ$	✓ Statement ✓ Reason ✓ Reason ✓ Statement ✓ Statement (5)
7.2.5	$\hat{R}_2 = 38^\circ$ and $\hat{P}_1 = 17^\circ$ $\therefore \hat{R}_2 \neq \hat{P}_1$ (alternate angles are not equal)	✓ Alternate angles are not equal or $\hat{R}_2 \neq \hat{P}_1$ or $\hat{R}_2 = 38^\circ$ and $\hat{P}_1 = 17^\circ$ (1)
		[13]

QUESTION 8

8.1	divides the other two sides proportionally	✓ Answer (1)
8.2.1	$\frac{x}{8} = \frac{4}{10}$ $10x = 32$ $x = 3,2$	✓ Prop. ✓ Simplification ✓ Value of x (3)
8.2.2	RTSP is a parallelogram (both pairs of opposite sides of a quadrilateral are parallel)	✓ Statement ✓ Reason (2)
8.2.3	$\frac{y}{9} = \frac{3,2}{8}$ Prop. Theorem ; TS MP $y = 3,6$	✓ Statement ✓ Reason ✓ Value of y (3)
8.2.4	$\frac{MR}{TS} = \frac{10}{4} = 2,5$ $\frac{RT}{SN} = \frac{9}{3,6} = 2,5$ $\frac{MT}{TN} = \frac{8}{3,2} = 2,5$ $\Delta MRT \parallel \Delta TSN$ sides of triangle are in the same proportion	✓ Ratio ✓ Ratio ✓ Ratio ✓ Reason (4)
		[13]

QUESTION 9

9.1	$\hat{K}_1 = \hat{LHF}$ ext $\angle$ of cyclic quad $= \hat{GFK}$ corres. angles $LK \parallel GF$	✓ Statement ✓ Reason ✓ Statement/Reason (3)
9.2	$\hat{MFG} = \hat{K}_1 = 104^\circ$ corres $\angle$ s; $FG \parallel KL$ $\hat{G} + 104^\circ + 20^\circ = 180^\circ$ angles of Δ $\hat{G} = 56^\circ$ $\hat{MFG} = \hat{K}_1 = 104^\circ$ corres. $\angle$ s; $FG \parallel KL$ $\hat{G} + 104^\circ + 20^\circ = 180^\circ$ angles of Δ $\hat{G} = 56^\circ$ OR $\hat{MLK} + 104^\circ + 20^\circ = 180^\circ$ angles of Δ $\angle$ s; $FG \parallel KL$ $\hat{MLK} = 56^\circ$ $\hat{MLK} = \hat{G}$ corresp $\angle$ s; $FG \parallel KL$ $\hat{G} = 56^\circ$	✓ Statement ✓ Statement ✓ Reason ✓ Statement ✓ Statement ✓ Reason (3)
9.3.1	$\frac{10}{30} = \frac{12}{MG}$ $MG = \frac{360}{10} = 36$ units (Prop. Theorem; $KL \parallel FG$)	✓ Statement ✓ Reason ✓ 36 units (3)
9.3.2	$\hat{MHF} = \hat{GFM} = 104^\circ$ proved in question 9.1. $\hat{M}$ is common $\hat{G} = \hat{F}_2$ sum of angles of a Δ $\Delta MFH \parallel \Delta MGF$ $\angle$; $\angle$; $\angle$	✓ Statement ✓ Statement and reason ✓ Reason (3)
9.3.3	$\Delta MFH \parallel \Delta MGF \parallel \Delta MLK$	✓ ΔMLK (1)
		[13]

QUESTION 10

10.1	$x^2 - 4dh + 4h^2 = 0$ $x^2 - (4 \times 220 \text{ mm} \times 60 \text{ mm}) + 4(60 \text{ mm})^2 = 0$ $x^2 = \sqrt{67200 \text{ mm}^2}$ $\therefore x = 259,23 \text{ mm}$	✓ Formula ✓ Substitution. ✓ Simplifying ✓ Length (4)
10.2.1	$v = \pi Dn$ $= \pi(18 \text{ m})(\frac{225}{60 \text{ s}})$ $\approx 212,06 \text{ m/s}$	✓ Correct formula ✓ Correct diameter ✓ Substitution ✓ 212,06 m/s (4)
10.2.2	$\omega = 2\pi n$ $= 2\pi(\frac{225}{60 \text{ s}})$ $\approx 23,56 \text{ rad/s}$	✓ Correct formula ✓ Substitution ✓ 23,56 rad/s (3)
10.3.1	$\hat{\text{LBA}} = 180^\circ - 70^\circ = 110^\circ$ co-int.angles; AK // BL	✓ Statement ✓ Reason (2)
10.3.2	$\hat{\text{KAD}} = 360^\circ - 140^\circ = 220^\circ$ $\approx 3,84 \text{ rad}$ $s_1 = r\theta = 50(3,84)$ $\approx 192 \text{ cm}$ $s_2 = 48,8 \text{ cm}$ Length of belt = $110 + 192 + 110 + 48,80$ $= 460,80 \text{ cm}$	✓ Size of $\hat{\text{KAD}}$ ✓ Conversion to radians ✓ Correct substitution in arc length formula ✓ Arc length s_1 ✓ Length of DE = 110 ✓ Length of belt (6)
		[19]

QUESTION 11

11.1.1	Volume of pyramid $= \frac{1}{3}(\text{area of base})(\text{height})$ $= \frac{1}{3}(4m \times 4m)(1,1m)$ $= 5,87m^3$ Volume of Cube $= (l)(b)(h)$ $= (4m)(4m)(4m)$ $= 64m^3$ Total Volume = $5,87m^3 + 64m^3$ $\approx 69,87m^3$	✓ Substitution in correct formula ✓ Height ✓ $5,87m^3$ ✓ Substitution in correct formula ✓ $64m^3$ ✓ $69,87m^3$ (6)
11.1.2	total surface area = surface area of cube base + surface area of pyramid $= 4(\text{side} \times \text{side}) + 4\left(\frac{1}{2} \times \text{base} \times \text{slant height}\right)$ $= 4(4m \times 4m) + 4\left(\frac{1}{2} \times 4m \times \sqrt{1,1^2 + 2^2}m\right)$ $= 64m^2 + 4(2m \times \sqrt{5,1}m)$ $= 82,07m^2$	✓ Slant height ✓ Correct substitution into area of a cube ✓ Correct substitution into area of pyramid ✓ Simplification ✓ Total area (5)
11.1.3	Cost of paint = $82,07 \times R30,50$ $= R2503,14$	✓ $82,07 \times R30,50$ ✓ R2503,14 (2)

11.2	$A_T = a \left(\frac{o_1 + o_n}{2} + o_2 + o_2 + o_3 + \dots o_{n-1} \right)$ $= 4 \left(\frac{6,2 + 2}{2} + y + 5,1 + 4,9 \right)$ $= 4(14,1 + y)$ $= 56,4 + 4y$ $\therefore 72 = 56,4 + 4y$ $\Rightarrow y = \frac{15,6}{4}$ $= 3,9m$ OR $A_T = a(m_1 + m_2 + m_3 + \dots m_n)$ $72 = 4 \left(\frac{6,2 + y}{2} + \frac{y + 5,1}{2} + \frac{5,1 + 4,9}{2} + \frac{4,9 + 2}{2} \right)$ $18 = \frac{11,3 + 2y}{2} + 8,45$ $9,55 = \frac{11,3 + 2y}{2}$ $19,1 = 11,3 + 2y$ $\therefore y = 3,9m$	✓ Formula ✓ Substitution ✓ Simplification ✓ 3,9m OR ✓ Formula ✓ Substitution ✓ Simplification ✓ 3,9m (4)
		[17]

TOTAL: 150